

QA1, QA2, QB3

48+2

70

Statics → First

Palestine Technical University

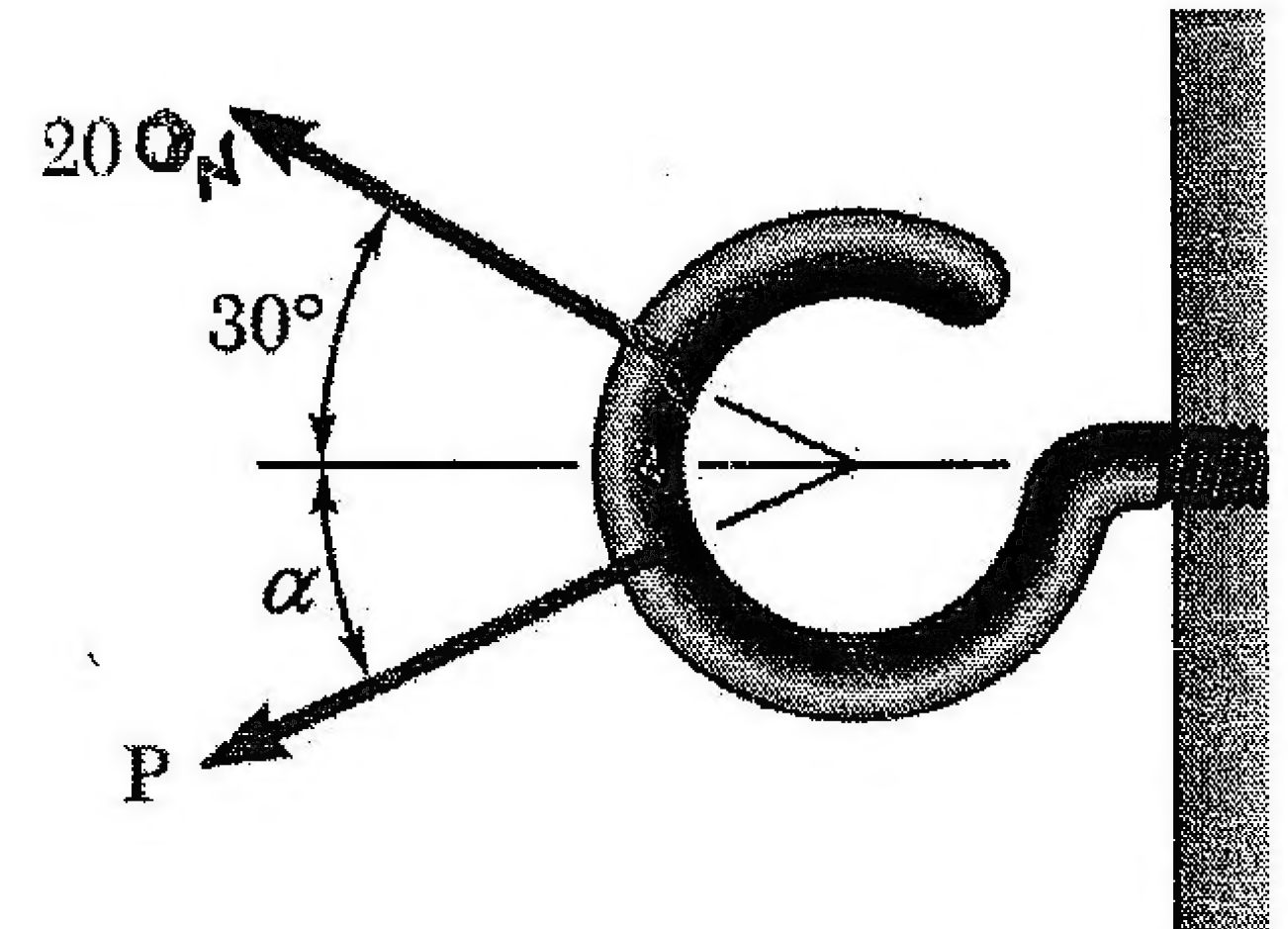
Maen Qedran

Statics Test 1 (This test carries 25% of the overall mark) -Your Name: م.ن. قدرانGroup: ☐ Mechatronics ☒ ElectricalAttempt 2 questions from section A and only 2 questions from section B**Section A: Multiple Choice - You must show your working out**

Date: 10.26.2010

QA1

Two forces are applied as shown to a hook support as shown. One of the forces is 200N and makes an angle of 30° with the horizontal while P makes an angle of α . Use trigonometry or otherwise, determine:



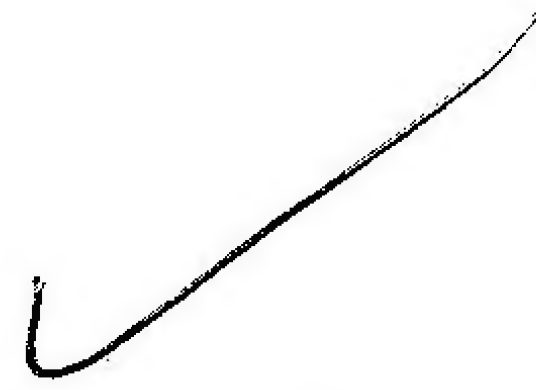
(a) The magnitude of the smallest force P for which the resultant R of the two forces applied to the support is horizontal, (b) the corresponding magnitude of R . Choose one of the following answers:

a) $P=10\text{ N}, R=17.32\text{ N}$

b) $P=100\text{ N}, R=153.2\text{ N}$

c) $P=110\text{ N}, R=173.2\text{ N}$

d) $P=100\text{ N}, R=173.2\text{ N}$



$$\frac{10}{10}$$

(20 marks)

a) **Solution**

$$\sum F_y = 0$$

Smallest force

$$\alpha = 90^\circ$$



$$200 \sin 30 - P \sin \alpha = 0$$

$$200 \sin 30 = P \sin \alpha$$

$$100 = P \sin 90$$

$$P = 100\text{ N}$$

$$\frac{10}{10}$$

b)

$$R = \sum F_x = 200 \cos 30 + 100 \cos 90$$

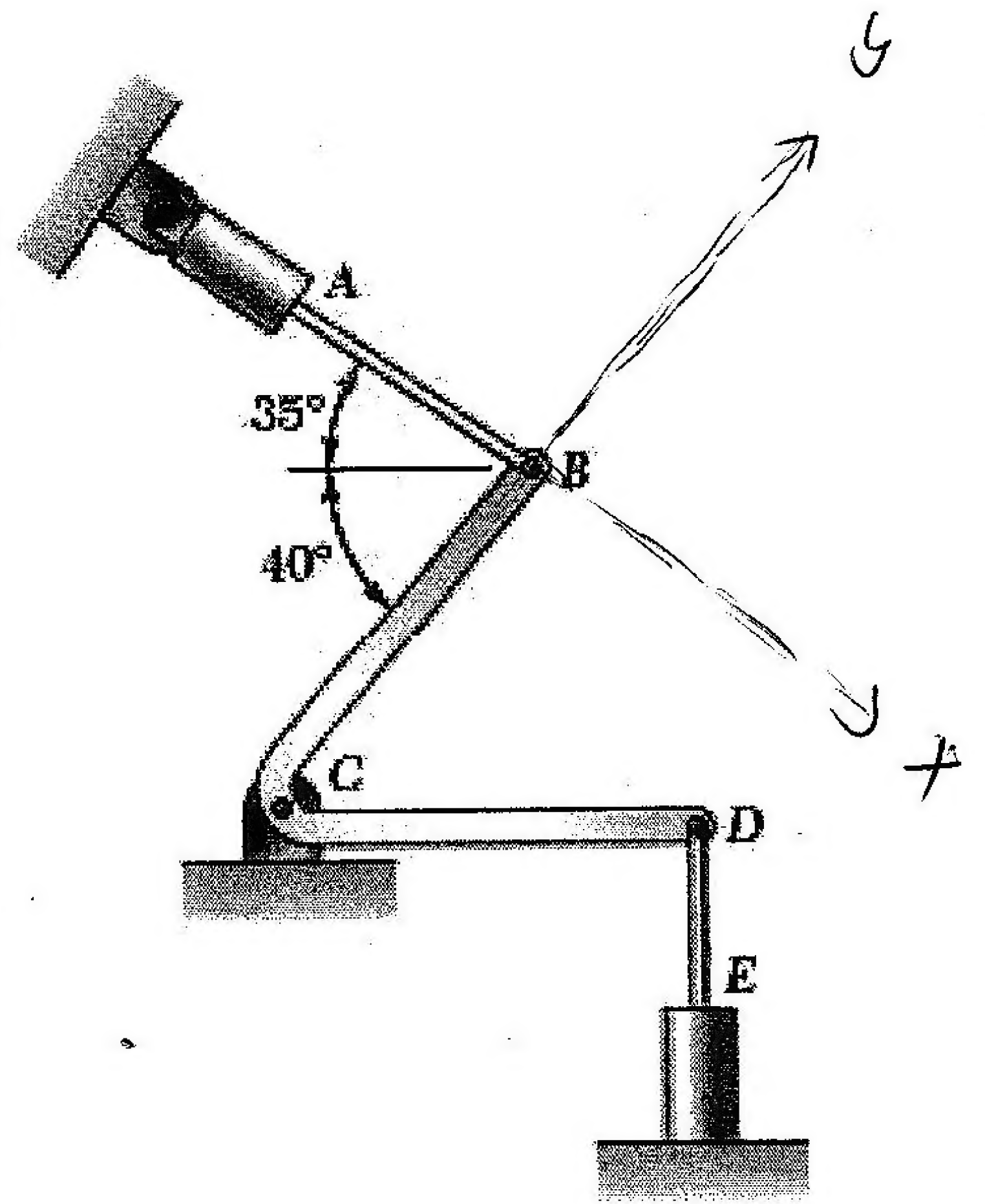
$$= 200 (0.866) + 0 = 173.2\text{ N}$$

تم الرفع بواسطة م.ن. قدران

Page 1

QA2 (Section A)

Activator rod AB exerts on crank BCD a force **P** directed along line AB. Draw the FBD for members AB and BCD. Also, knowing that **P** must have a 250 N component perpendicular to arm BC of the crank, determine:



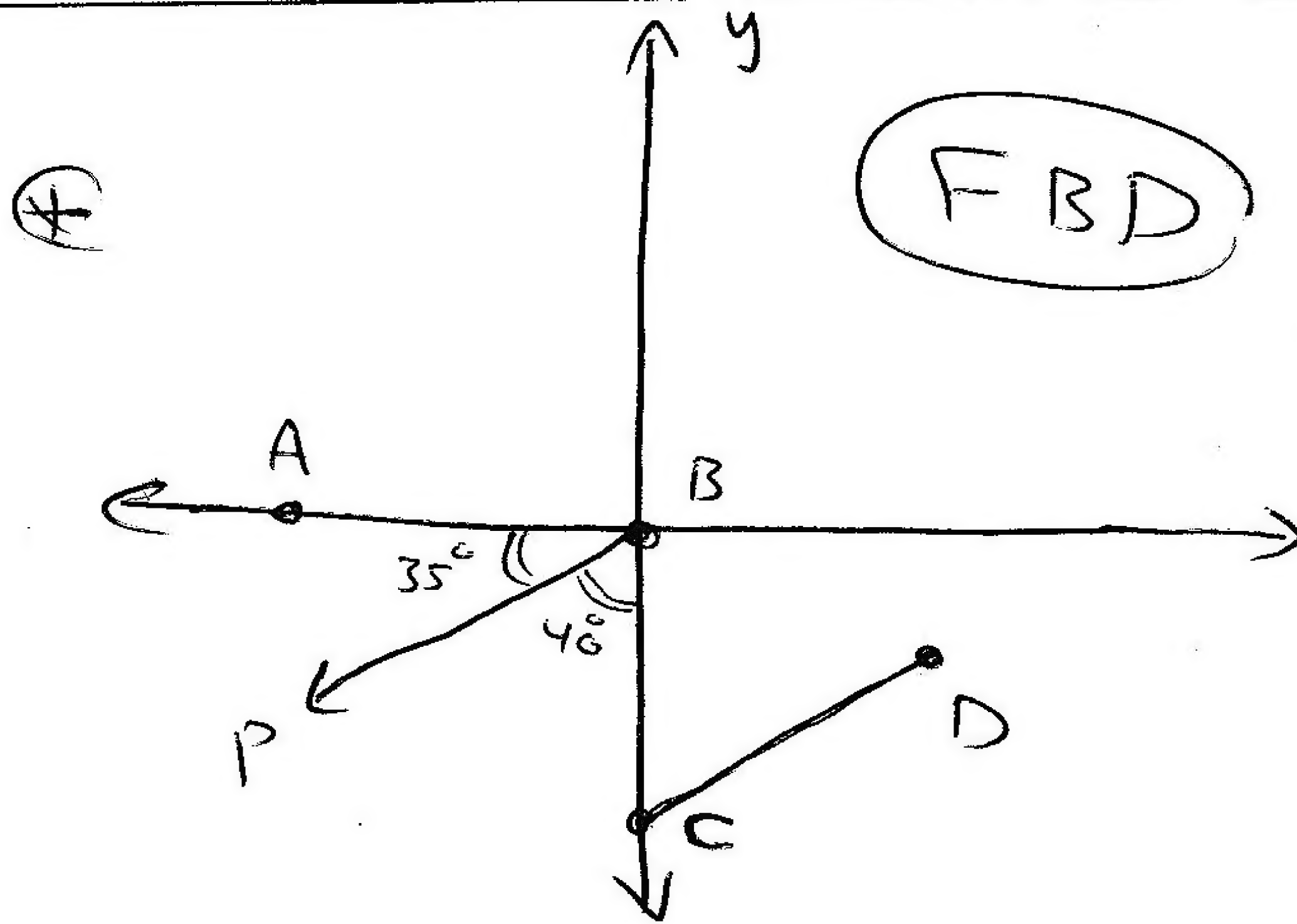
- The magnitude of the force **P**,
- Its component (P_{BC}) along BC [assume BC is straight].

Select one answer from the following answers:

- $P = 25.9 \text{ N}$, $P_{BC} = 57 \text{ N}$
- $P = 259 \text{ N}$, $P_{BC} = 67 \text{ N}$
- ☒ $P = 239 \text{ N}$, $P_{BC} = 6.7 \text{ N}$
- $P = 259 \text{ N}$, $P_{BC} = 670 \text{ N}$

X 0/10
(20 marks)

Solution



~~$250 = P \cos 40$~~ $\rightarrow P = \frac{250}{\cos 40}$
 ~~$250 = 239$~~

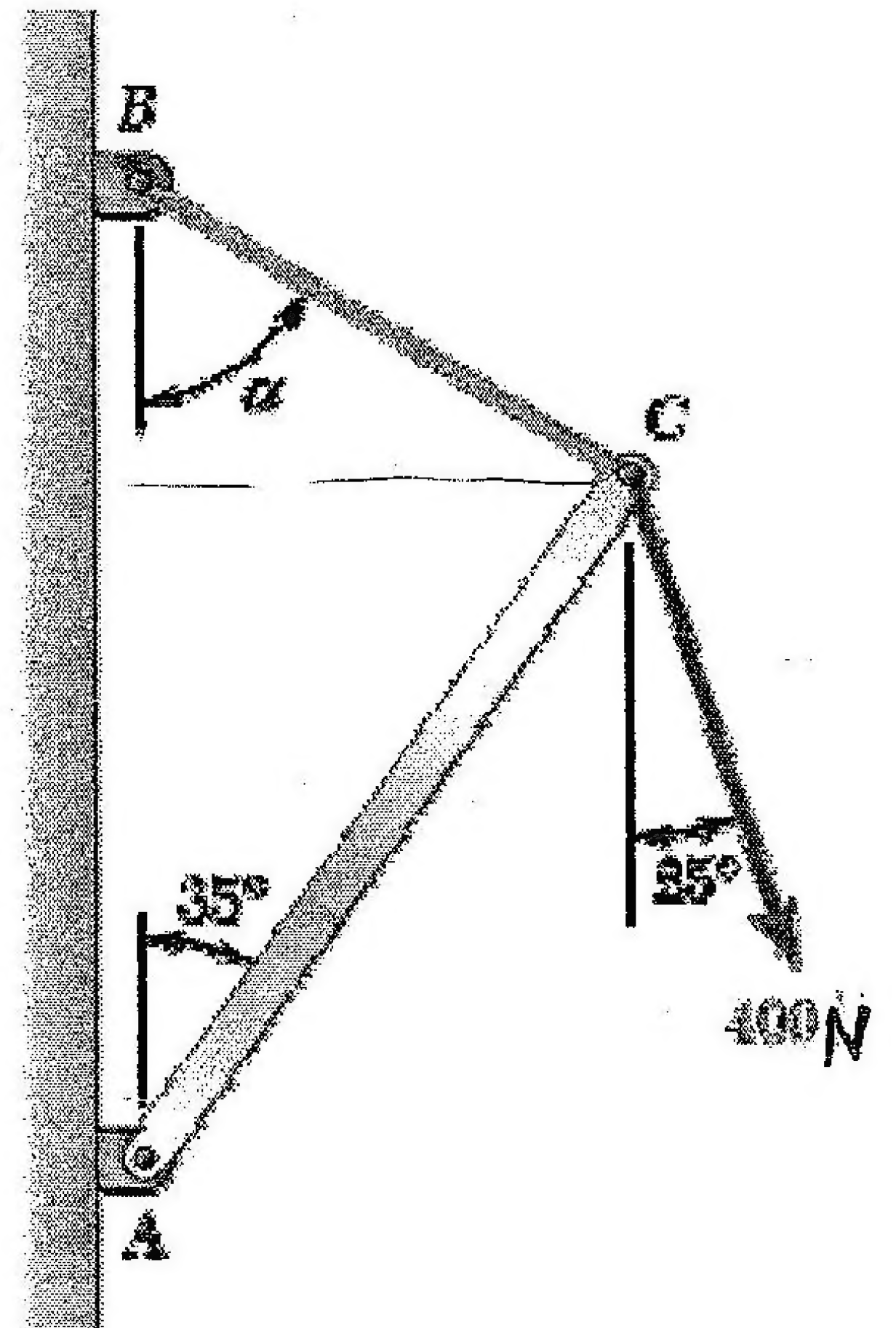
0/20

Section B (You need to answer **ANY 2** questions only from this section)

QB1

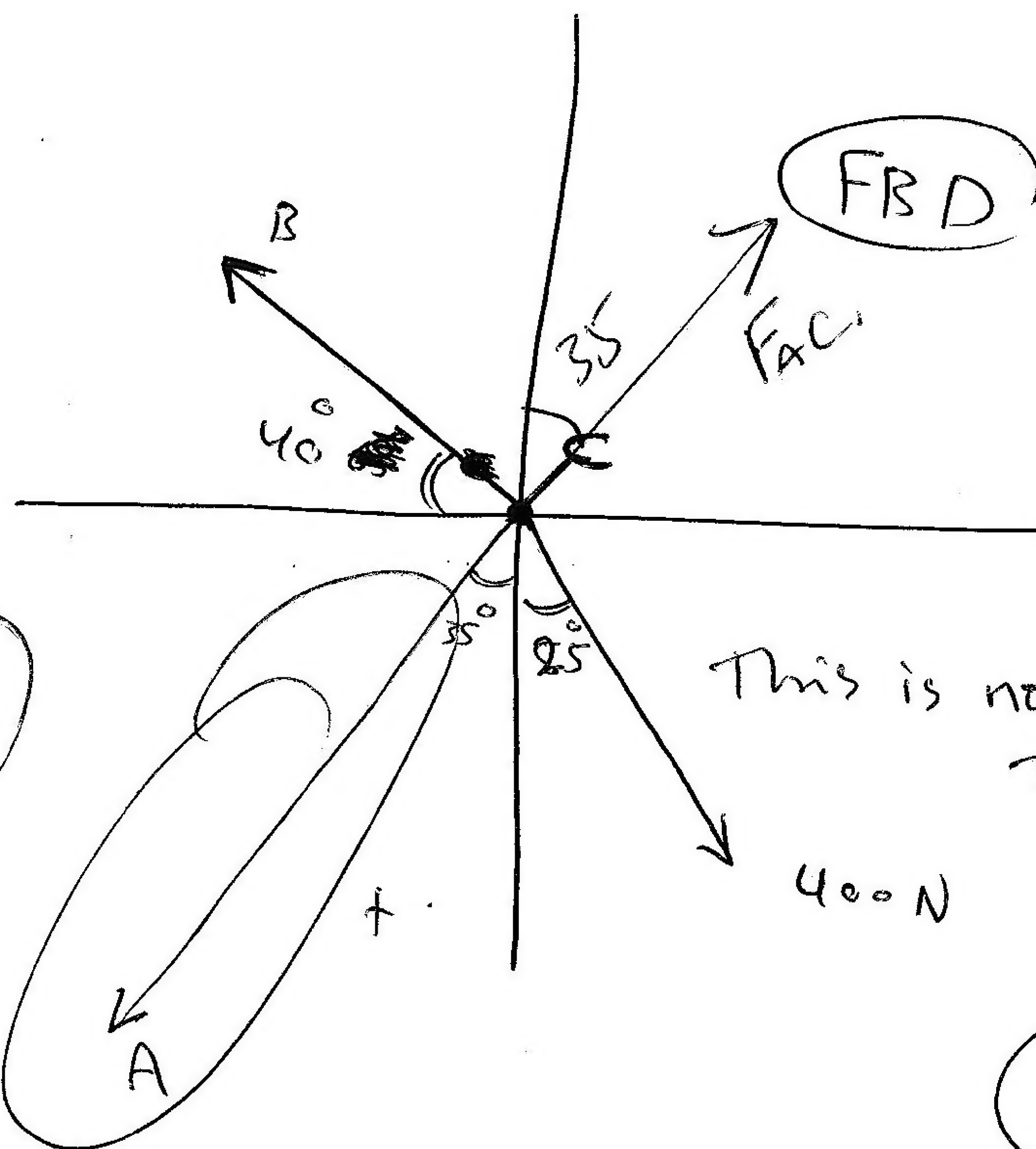
A uniform beam, AC, is held in the position, as shown in the diagram, by a cable BC which is inclined by an angle of $\alpha = 50^\circ$ with the vertical. A force of 400 N is applied at point C, making an angle of 25° with the vertical. The pin at A exerts a force on AC directed along line AC. For this system:

- Sketch the Free Body Diagram of the beam AC showing ALL forces. (5 marks)
- By using accurate drawing of forces (or otherwise), determine the magnitude of the force in AC (15 marks)
- Find the tension in the cable BC (10 marks)



Solution

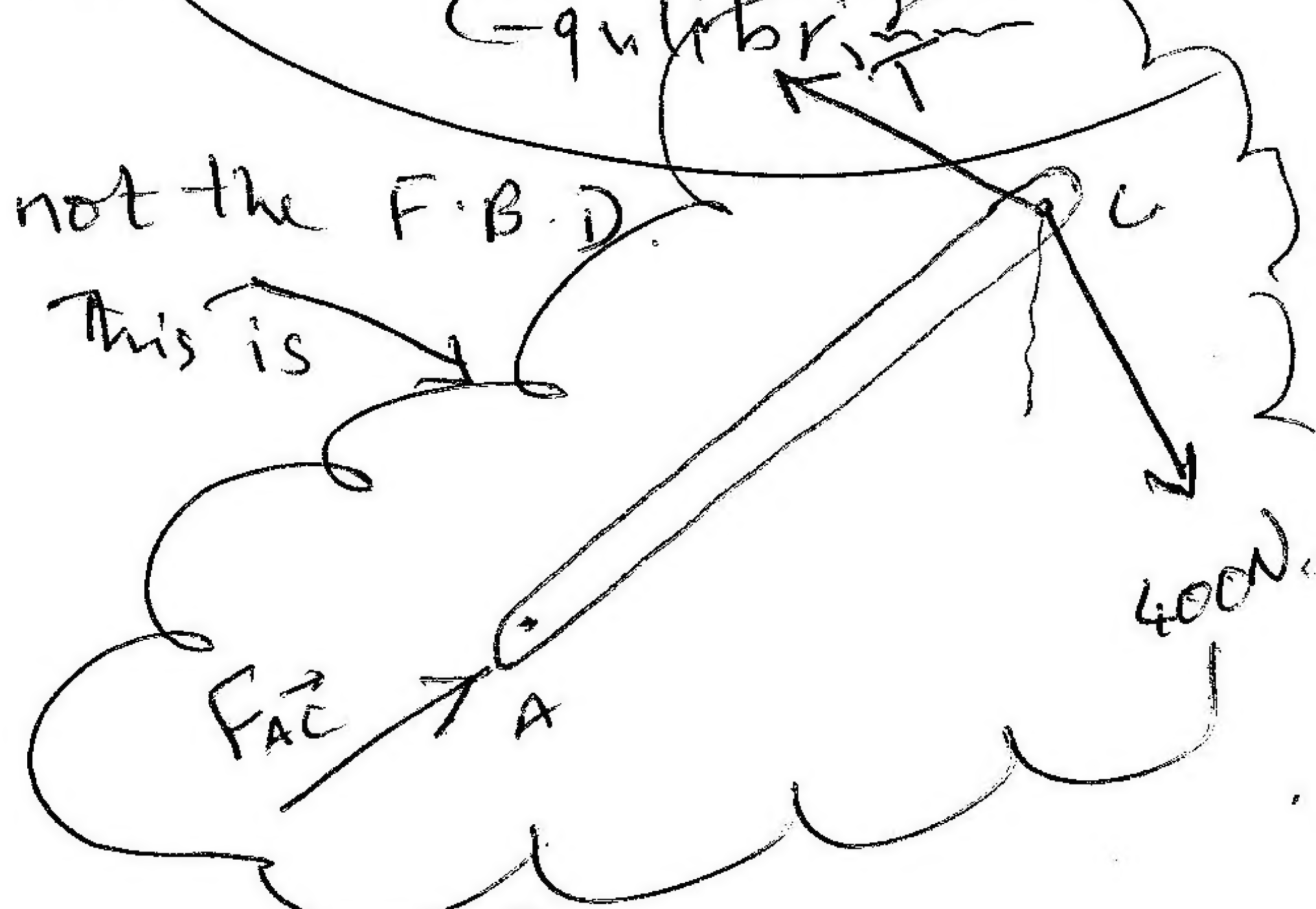
a



This system is in Equilibrium

This is not the F.B.D.

This is



b

$$\sum F_x = -BC \cos 40^\circ - AC \sin 35^\circ + 400 \sin 25^\circ = 0$$

~~-B~~

$$-0.77 BC - 0.57 AC + 169 = 0 \quad \text{--- (1)}$$

$$\sum F_y = BC \sin 40^\circ - AC \cos 35^\circ - 400 \cos 25^\circ = 0$$

$$0.64 BC - 0.82 AC - 362.5 = 0$$

$$0.64 BC - 0.82 AC = 362.5 \quad \text{--- (2)}$$

But ~~BC~~ $BC = \frac{362.5 + 0.82 AC}{0.64}$

$$BC = \frac{566.4 + 1.28 AC}{0.64}$$

$$\therefore -0.77(566.4 + 1.28 AC) - 0.57 AC + 169 = 0$$

$$-436.1 - 0.98 AC - 0.57 AC + 169 = 0$$

$$-1.55 AC - 267.1 = 0$$

$$1.55 AC = -267.1 \Rightarrow AC = \frac{-267.1}{1.55}$$

$$= \boxed{-172.3 \text{ N}}$$

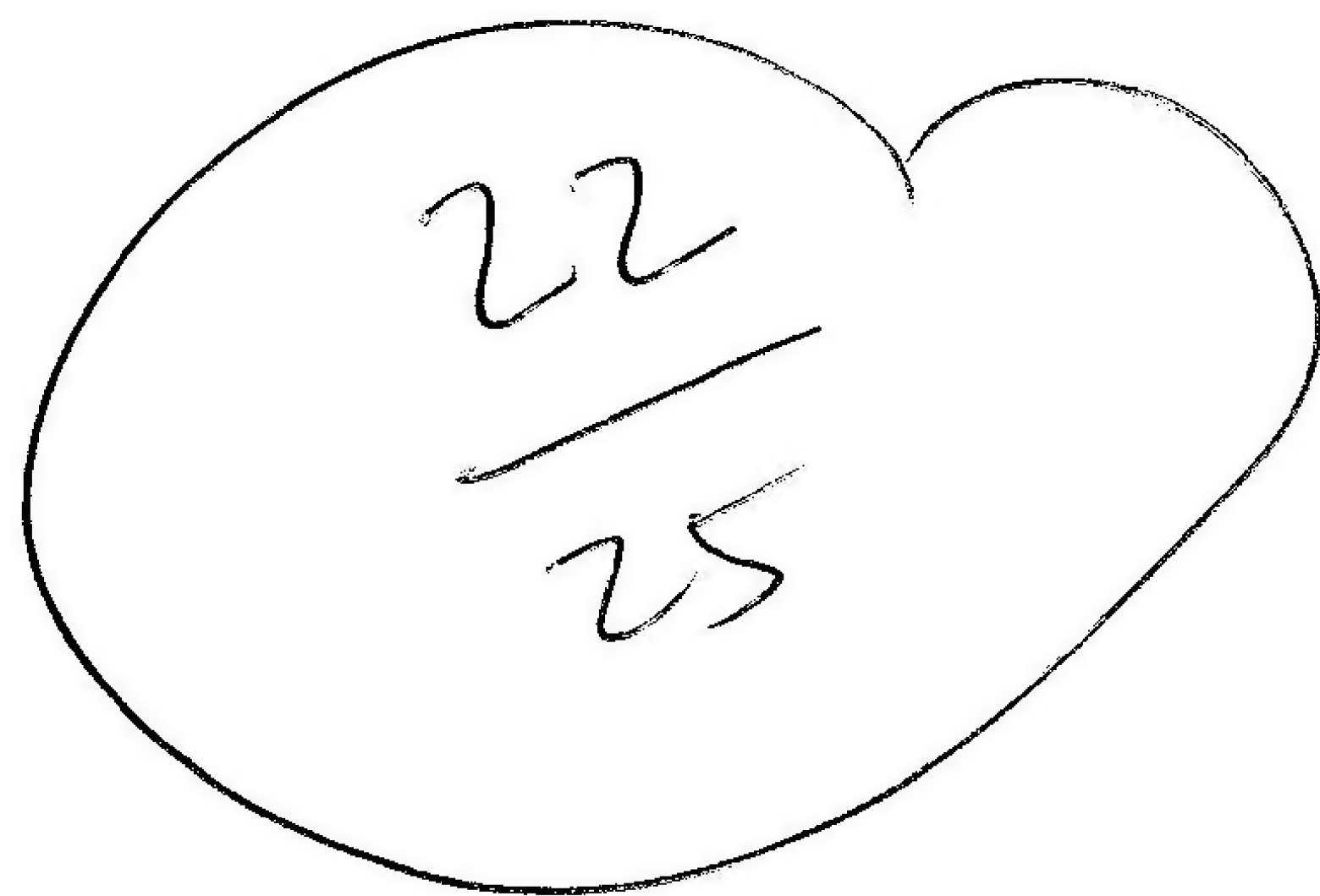
But F_{AC} is not
in the -ve direction.

$$c) BC = 566.4 + 1.28(-172.3)$$

$$= 566.4 + (-220.5)$$

$$= \boxed{345.9 \text{ N}}$$

Your workout could be
right if you have chosen
the correct direction for BC.



QB2

Before a telephone cable is strung, rope BAC is tied to the stake at B and is passed over a pulley at A as shown in the diagram. If part AC of the rope lies in the plane parallel to the xy-plane and that the tension (T) in the rope is 130 N, find the following:

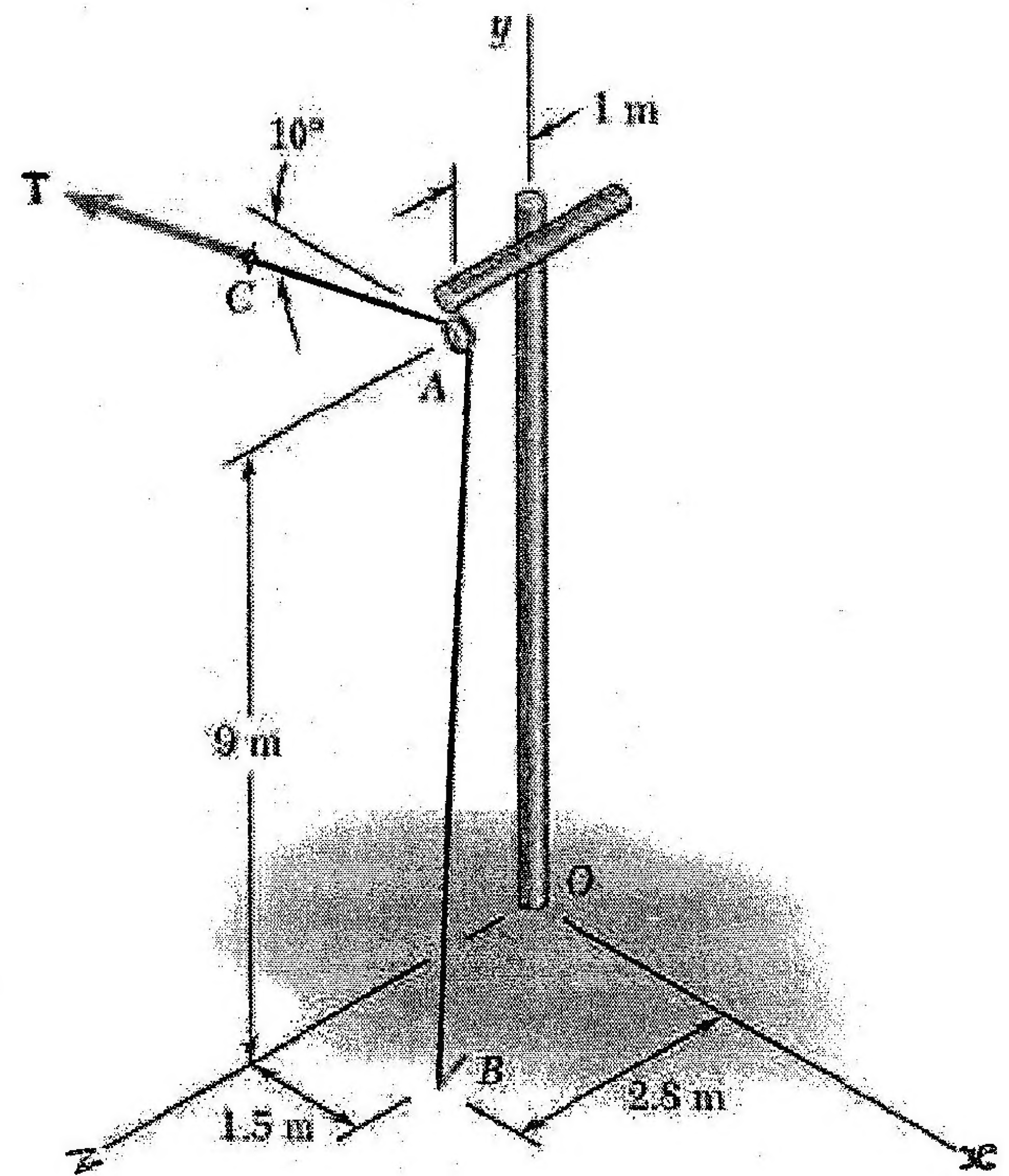
- a) The resultant force exerted on the pulley by the rope ends - in terms of the i, j & k

(15 marks)

- b) The moment of this resultant about an axis through point O (again in terms of i, j, k).

(15 marks)

Solution

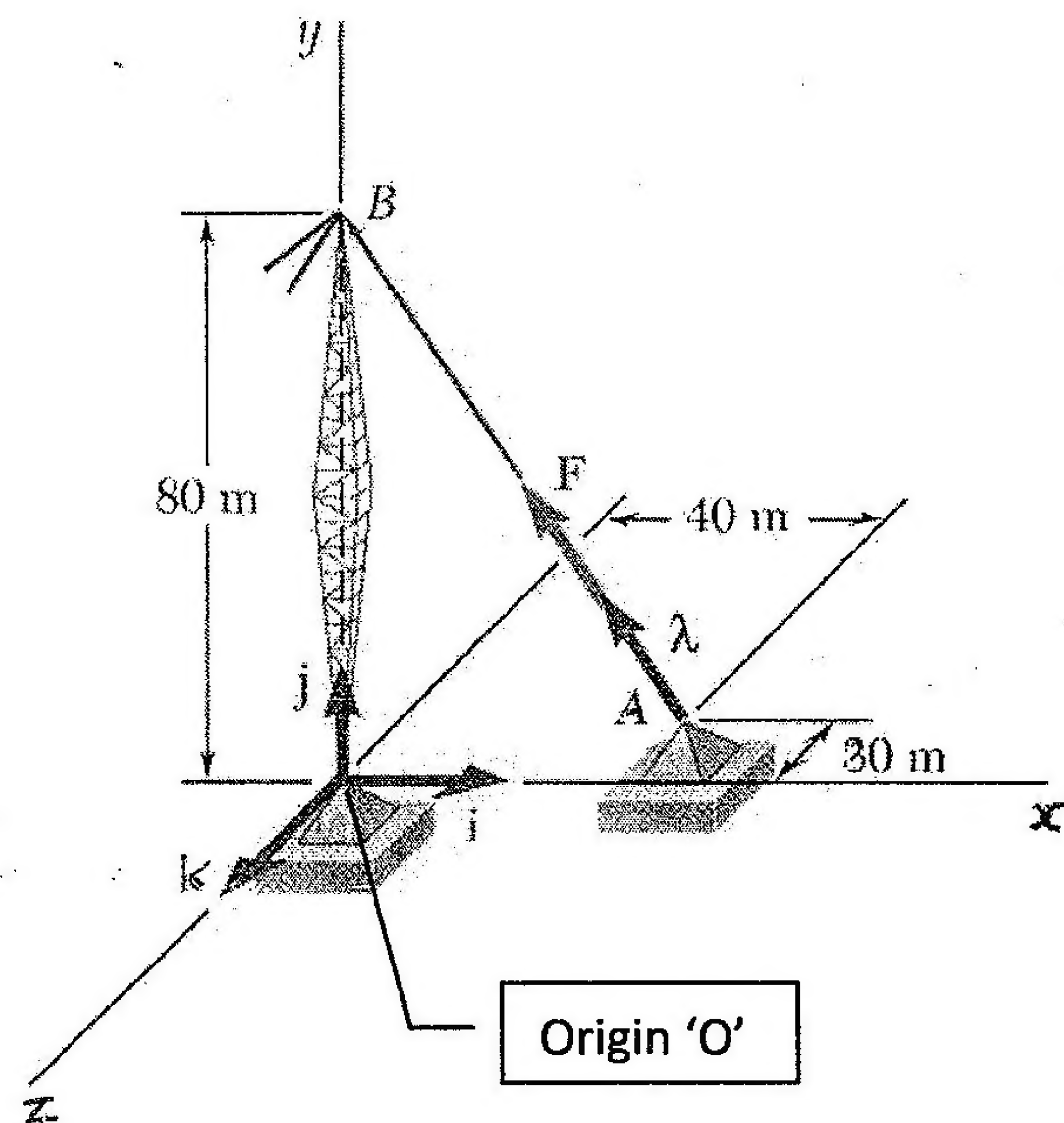


QB3

A winch tower, OB, is held vertically upwards by a system of 3 cables. The tower is supported at point (O) by a universal pin-joint while its top end (B) is held in position by the cables. The tension in cable BA is 3200 N. Determine:

a) The components F_x , F_y , F_z of the force acting on the bolt at A (in terms of i , j and k) (15 marks)

b) The moment of the force (F) about the origin 'O' (in terms of i , j and k) (15 marks)



a) $F = 3200 \text{ N}$

$$\vec{F} = \hat{\lambda} F$$

$$\hat{\lambda} = \frac{\vec{r}_{B/A}}{|\vec{r}_{B/A}|}$$

$$\vec{r}_{B/A} = \vec{r}_B - \vec{r}_A = 80\hat{j} - (40\hat{i} - 30\hat{k})$$

$$= -40\hat{i} + 80\hat{j} + 30\hat{k} \text{ m}$$

$$|\vec{r}_{B/A}| = \sqrt{(-40)^2 + (80)^2 + (30)^2} = \sqrt{1600 + 6400 + 900} = 94.3 \text{ m}$$

$$\hat{\lambda} = \frac{-40\hat{i} + 80\hat{j} + 30\hat{k}}{94.3} = -0.42\hat{i} + 0.85\hat{j} + 0.32\hat{k}$$

$$\vec{F} = 3200 (-0.42\hat{i} + 0.85\hat{j} + 0.32\hat{k})$$

$$= -1344\hat{i} + 2720\hat{j} + 1024\hat{k} \text{ N}$$

b) $M_o = \vec{r} \times \vec{F}$

$$\vec{r}_A = (40\hat{i} - 30\hat{k})$$

$$M_o = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 40 & 0 & -30 \\ -1344 & 2720 & 1024 \end{vmatrix}$$

خلف الصفحة

$$= i(81600) - j(40960 - (40320)) + k(108800)$$

$$= \boxed{81600i - 640j + 108800k} \quad \text{N.m}$$

81408

0j

108544

i if you were more accurate, you would have got the above results

$$\frac{13+2}{15}$$

